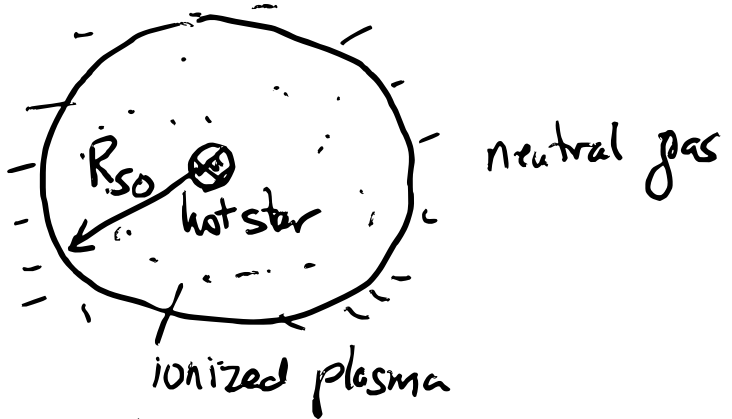
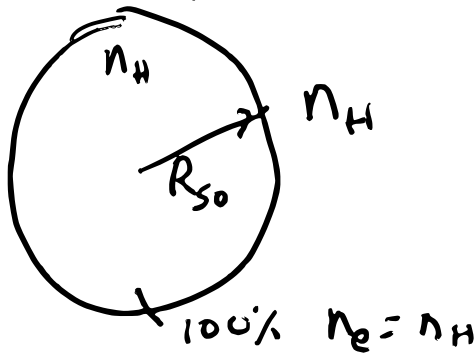


HII Regions

Classical HII regions: sharp boundaries



STROMGREN approximation



Q_0 : ~~rate~~ rate of photoionizing photons

$$Q_0 = n_e n_p \alpha \frac{4\pi R_{50}^3}{3}$$

(s^{-1}) ($cm^{-3} s^{-1}$)

$$n_e \approx n_p \approx n_H$$

$$R_{50} = \left(\frac{3Q_0}{4\pi n_H^2 \alpha} \right)^{1/3}$$

$$Q_0 = 10^{49} \text{ phot/s}$$

$$R_{50} = 3 \text{ pc } Q_{49}^{1/3} n_2^{-2/3} T_4^{0.28}$$

$$Q_{49} = \left(\frac{Q}{10^{49}} \right) \quad n_2 = \frac{n_H}{10^2 \text{ cm}^{-3}} \quad T_4 = \frac{T}{10^4 \text{ K}}$$

Hot white dwarf: $2 \times 10^4 \text{ K}$

$$\text{WNM: } n_H = 1 \text{ cm}^{-3}$$

$$\text{CNM: } n_H = 50 \text{ cm}^{-3}$$

EM = column of $n_e n_p$

$$= \int n_e n_p dl \approx n_e^2 L$$

$$\approx n_H^2 2R_{50}$$

$$\text{EM} = n_H^2 R_{50}$$

$$= 4.2 \times 10^4 Q_{49}^{1/2} n_2^{1/2} T_4^{0.28} \text{ cm}^{-6} \text{ pc}$$

$$T \leq 50,000 \text{ K}$$

$$h\nu \approx 18 \text{ eV}$$

Mean-free path in ISM

$$\sigma_{\text{pi}}(h\nu = 18 \text{ eV}) \approx 3 \times 10^{-18} \text{ cm}^2$$

$$\text{mfp} = \frac{1}{n_{\text{H}} \sigma_{\text{pi}}} = 3.4 \times 10^{17} \text{ n}^{-1} \text{ cm}$$

$$\begin{aligned} &\leftarrow \text{pc} \\ &\approx 0.1 \text{ n}^{-1} \text{ pc} \end{aligned}$$

$$\approx 10^{-3}$$

$$R_{50} \approx 3 \text{ pc}$$


$$\text{mfp} \approx \underline{\underline{10^{-3} \text{ pc}}}$$

Time to ionize an HII region?

$$t_{\text{ionization}} \times Q_0 = \underbrace{\frac{4\pi R_{51}^3}{3} n_H}_{\text{Volume} \times \text{Density}}$$

$$t_{\text{ion}} \propto \frac{1}{\alpha_B n_H}$$

Timescale for recombination (α "case B")

$n_e n_p \alpha_B$ 

$$t_{\text{recomb}} \times n_e n_p \alpha_B = n_H$$

$$n_e = n_p = n_H$$

$$t_{\text{recomb}} = \frac{1}{\alpha_B n_H}$$

$$t_{\text{rec}} = \frac{1.2 \times 10^3 \text{ yr}}{(n_H / 100 \text{ cm}^{-3})}$$

Case A, case B:

The photo-electron ionization cross-section is

$$\sigma_{pi} \approx \sigma_0 \left(\frac{\nu}{\nu_0} \right)^{-3}$$

\uparrow
 $6 \times 10^{-18} \text{ cm}^{-2}$

$h\nu_0 = 13.6 \text{ eV}$

Consider a typical HII region,

$$n_H \approx 10^2 \text{ cm}^{-3}, \quad L \approx 1 \text{ pc.}$$

The $\tau_{pi} = n_H L \sigma_{pi} \gg 1$

Any recombination to $n=1$ results in $h\nu > 13.6 \text{ eV}$ photon. It will get absorbed in the vicinity of emission

\Rightarrow "on the spot absorption"

Case B: Do not include recombination to $n=1$

Case A: Include all recombinations

Lyman- α & Two-photon continuum:

Consider recombination to $n=2$.

$$2s \text{ --- } 2s_{1/2} \quad 2p \text{ === } 2p_{1/2, 3/2}$$

$$1s \text{ =====}$$

About $\frac{1}{3}$ will be to $2s \ 2s_{1/2}$ and $\frac{2}{3}$ to $2p \ 2p$

- o The latter decay rapidly to produce Ly α .
- o The former decay ~~to~~ via 2-photon continuum.

However, if the density of protons is high the $2s \rightarrow 2p$ transition can take place \Rightarrow Ly α .

Ly-series has large cross-section

	$\lambda(\text{\AA})$	$A(s^{-1})$	$\frac{f_{lu}}{A}$
Ly α	1216	6.2×10^8	0.4164
Ly β	10256	1.6×10^8	0.0791
Ly γ	972	6.8×10^7	0.0290
Ly δ	950	3.4×10^7	0.0139

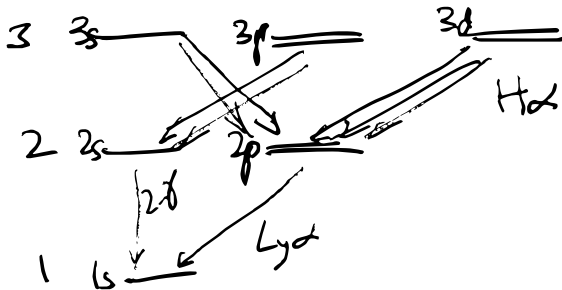
$$\text{Ly}\alpha: \tau_0(\text{Ly}\alpha) = 0.758 \left(\frac{N_e}{10^{13} \text{ cm}^{-2}} \right) \left(\frac{f_{lu}}{0.4164} \right) \left(\frac{\lambda}{1216 \text{\AA}} \right) \left(\frac{v}{10^6 \text{ m/s}} \right)$$

So Ly- α will rattle around the H II region.

It will

- be destroyed by dust (if present is sufficient qty)
- "random walk" out of the H II region.

Ly β : Consider recomb to $n=3$



Real-life complications:

o Dynamics.

$$h\nu = 18 \text{ eV}$$

$$\Delta E = h\nu - IP = 18 - 13.6 \text{ eV} \\ = 4.4 \text{ eV}$$

$$1 \text{ eV} = 10^4 \text{ K}$$

$$\downarrow 4.4 \times 10^4 \text{ K}$$

$$T \approx 8000 \text{ K}$$

$$V_{\text{rms}} = \sqrt{\frac{T}{121}} \text{ km s}^{-1}$$

$$V_{\text{rms}} = 10 \text{ km/s}$$

$$V_{\text{ion}} = \frac{3 \times 3 \times 10^{18} \text{ cm}}{10^3 \times 3 \times 10^7 \text{ s}} \\ = 3 \times 10^8 \text{ cm/s} \approx 0.01c$$

o DUST!