Are you MKIDing me?!

The Story of MUSIC's Detectors



Outline

- Introduction to Microwave Kinetic Inductance Detectors (MKIDs)
- Recap of the 2010 DemoCam Observing Run
- The problem of dark response
- The problem of low optical efficiency
- Results from the latest 6x6 (4 Color) Array
- o Future work

MUSIC

576 spatial pixels, simultaneously sensitive to
 4 spectral bands

ν (GHz)	150	230	290	350
Δν (GHz)	34	45	34	21

- o 14 arcminute FOV
- Primary science goals:
 - Pointed observations of galaxy clusters through the tSZ Effect
 - Wide blank-field surveys of dusty, star-forming galaxies
- First camera at any wavelength to use MKIDs as detectors
- Scheduled to be commissioned at the CSO in the winter of 2011/2012



Photo courtesy of Matt Hollister

Introduction to MKIDs

Superconductivity

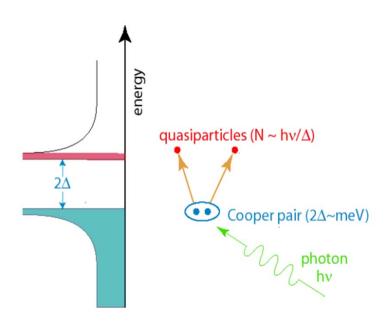
- A Cooper pair consists of two electrons bound together by the electronphonon interaction. The energy of the Cooper pair is below the Fermi energy.
- Binding energy is weak.

Aluminum:
$$\Delta \approx 0.18 \text{ meV}$$
 $\frac{2\Delta}{h} \approx 80 \text{ GHz}$

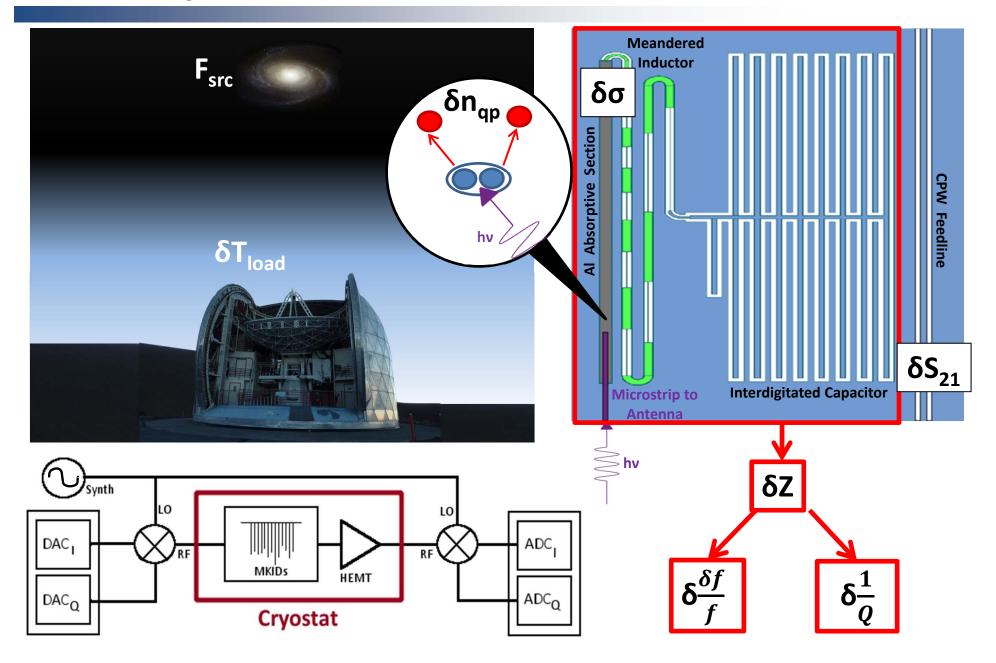
Niobium: 1.45 meV 700 GHz

- Still, prevents inelastic scattering resulting in zero DC resistance.
- But Cooper pairs have inertia. Results in a "phase-lag" between current and an AC electric field that has a form equivalent to an inductance:

Kinetic Inductance



Principle of Detection



Basics

- MKIDs are superconducting RLC circuits, capacitively coupled to a feedline.
- Near the resonant frequency the complex transmission S₂₁ of a microwave probe signal sweeps out a circle

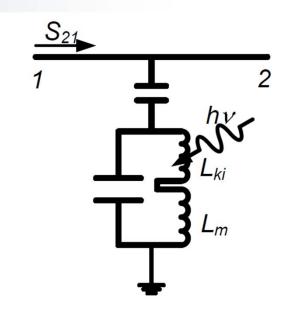
$$S_{21}(f) = 1 - \frac{Q/Q_c}{1 + 2iQ\frac{f - f_0}{f_0}}$$

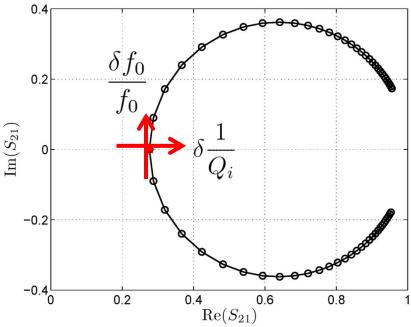
where

$$\frac{1}{Q} = \frac{1}{Q_i} + \frac{1}{Q_c}$$

 Consider small perturbations in frequency and loss, this results in perturbations in the transmission on resonance given by

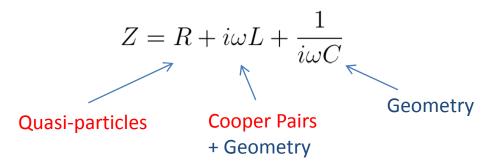
$$\delta S_{21} = \frac{Q^2}{Q_c} \left(\delta \frac{1}{Q_i} - 2i \frac{\delta f_0}{f_0} \right)$$
 Amplitude Phase





Basics

o The frequency f and loss 1/Q are determined by the impedance of the circuit



Define the kinetic inductance fraction

$$\alpha = \frac{L_k}{L} = \frac{L_k}{L_k + L_m}$$

o Frequency and loss then given by

$$f_0 \propto \frac{1}{\sqrt{LC}}$$

$$\delta f_0 = f_0 \left(\frac{\sqrt{L}}{\sqrt{L + \delta L}} - 1 \right) = -\frac{f_0}{2} \frac{\delta L}{L}$$

$$\frac{\delta f_0}{f_0} = -\frac{\alpha}{2} \frac{\delta L_k}{L_k}$$

$$\frac{1}{Q_i} \ = \ \frac{R}{\omega L}$$

$$\delta \left(\frac{1}{Q_i} \right) = \alpha \frac{\delta R}{\omega L_k}$$

Basics

 Changes in resistance and inductance of the resonator due solely to changes in the complex conductivity of the superconductor

$$\sigma = \sigma_1 - i\sigma_2$$

For a superconducting thin film

$$\frac{\delta Z_s}{Z_s} = \frac{\delta \sigma}{\sigma}$$

Lets measure relative to the values at zero temperature, so that

$$\sigma_1(0) = 0$$

$$R(0) = 0$$

and

$$\frac{\delta R}{\omega L_k(0)} = \frac{\delta \sigma_1}{\sigma_2(0)} \qquad \frac{\delta L_k}{\omega L_k(0)} = -\frac{\delta \sigma_2}{\sigma_2(0)}$$

 Now just need a theory for the complex conductivity of a thin superconducting film under an AC electromagnetic field.

Mattis - Bardeen Theory

o In 1958, D.C. Mattis and J. Bardeen use BCS theory to derive an expression for the complex conductivity

$$\sigma = \sigma_1 - i\sigma_2$$

of a superconducting thin film:

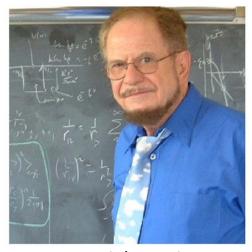
$$\frac{\sigma_1}{\sigma_n} = \frac{2}{\hbar\omega} \int_{\Delta}^{\infty} \frac{[f(E) - f(E + \hbar\omega)](E^2 + \Delta^2 + \hbar\omega E)}{\sqrt{E^2 - \Delta^2}\sqrt{(E + \hbar\omega)^2 - \Delta^2}} dE
+ \frac{1}{\hbar\omega} \int_{\Delta - \hbar\omega}^{-\Delta} \frac{[1 - 2f(E + \hbar\omega)](E^2 + \Delta^2 + \hbar\omega E)}{\sqrt{E^2 - \Delta^2}\sqrt{(E + \hbar\omega)^2 - \Delta^2}} dE
\frac{\sigma_2}{\sigma_n} = \frac{1}{\hbar\omega} \int_{\max\{\Delta - \hbar\omega, -\Delta\}}^{\Delta} \frac{[1 - 2f(E + \hbar\omega)](E^2 + \Delta^2 + \hbar\omega E)}{\sqrt{\Delta^2 - E^2}\sqrt{(E + \hbar\omega)^2 - \Delta^2}} dE.$$

Here f(E) is the Fermi distribution

$$f(E; \mu^*, T) = \frac{1}{1 + e^{\frac{E - \mu^*}{kT}}}$$



John Bardeen



Daniel Mattis

Mattis – Bardeen Theory

o In the limits applicable to our detectors $\hbar\omega\ll\Delta$ and $kT\ll\Delta$ the first order approximation is valid

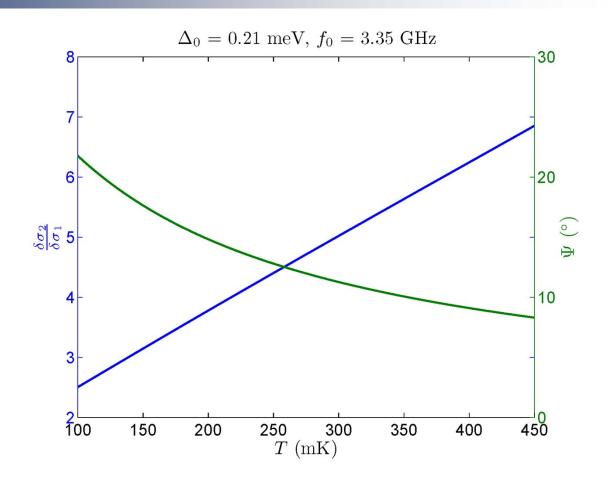
$$\frac{\delta \sigma_1}{\sigma_2(0)} = \frac{1}{\pi N_0} \sqrt{\frac{2}{\pi k T \Delta_0}} \sinh\left(\frac{\hbar \omega}{2kT}\right) K_0 \left(\frac{\hbar \omega}{2kT}\right) n_{qp} = \kappa_1(\omega, T, \Delta_0) n_{qp}$$

$$\frac{\delta\sigma_2}{\sigma_2(0)} = -\frac{1}{2\Delta_0 N_0} \left[1 + \sqrt{\frac{2\Delta_0}{\pi kT}} e^{-\frac{\hbar\omega}{2kT}} I_0 \left(\frac{\hbar\omega}{2kT} \right) \right] n_{qp} = \kappa_2(\omega, T, \Delta_0) n_{qp}$$

Hence, complex conductivity is proportional to quasi-particle density

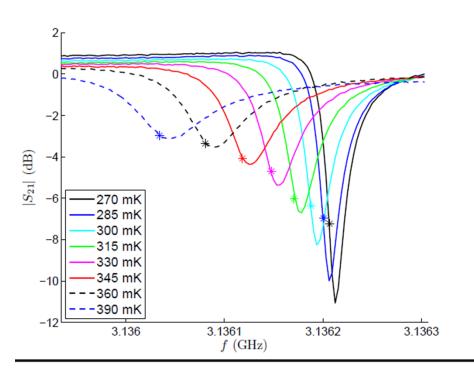
$$n_{qp} = 2N_0 \sqrt{2\pi kT} e^{\frac{\Delta - \mu^*}{kT}}$$

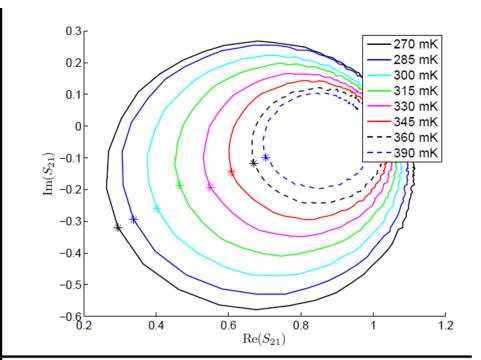
Mattis – Bardeen Theory

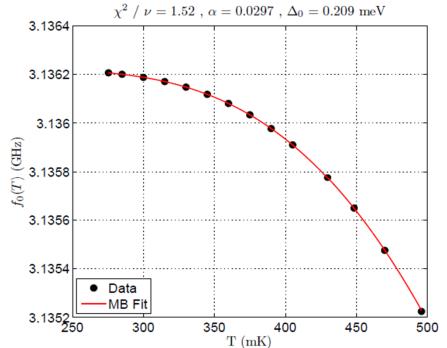


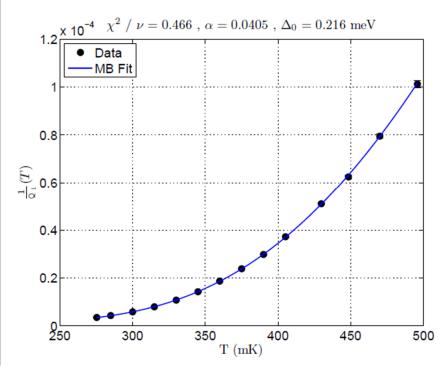
o Frequency response inherently larger than dissipation response

$$\frac{\delta \sigma_1}{\delta \sigma_2} = \frac{\kappa_1 (\omega, T, \Delta_0)}{\kappa_2 (\omega, T, \Delta_0)} = \tan (\Psi)$$



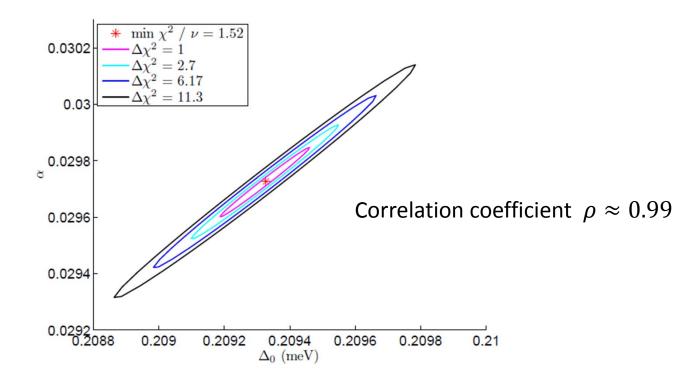






Mattis - Bardeen Theory

Obtain very good estimates of α and Δ_0 from MB fits to dark temperature sweeps

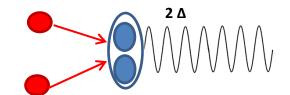


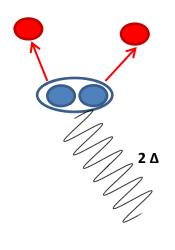
o However, results from fits to frequency and loss inconsistent.

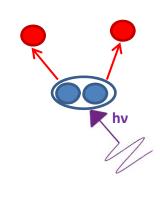
The G-R Equation

In a steady state

$$\Gamma_{th}^G + \Gamma_{opt}^G = \Gamma^R$$







Optical Generation

$$\Gamma_{opt}^{G} = \frac{\eta P}{\Delta} = \frac{\eta k (T_{load} + T_{exc}) B}{\Delta}$$

Recombination

$$\Gamma^R = \frac{V n_{qp}}{\tau}$$

where

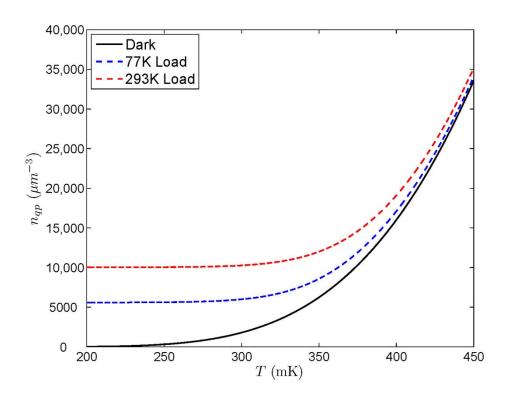
$$\frac{1}{\tau} = Rn_{qp} + \frac{1}{\tau_0}$$

$$n_{qp} = n_{qp,opt} + n_{qp,th}(T, \alpha, \Delta_0)$$

$$\Gamma_{th}^{G} + \frac{\eta k (T_{load} + T_{exc})B}{\Delta} = RV n_{qp}^{2} + \frac{V n_{qp}}{\tau_{0}}$$

Obtain the following quadratic equation for quasi-particle density

$$\frac{\eta k (T_{load} + T_{exc})B}{RV\Delta} = n_{qp}^2 - n_{qp,th}^2 + \frac{1}{R\tau_0} (n_{qp} - n_{qp,th})$$



Taking the derivative with respect to T_{load}

$$\frac{dn_{qp}}{dT_{load}} = \frac{\eta kB}{RV\Delta \left(2n_{qp} + \frac{1}{R\tau_0}\right)}$$

Responsivity

Responsivity =
$$\left[\frac{dS_{21}}{d(\frac{\delta f}{f})} \right] \left[\frac{d(\frac{\delta f}{f})}{d(\frac{\delta \sigma_2}{\sigma_2})} \right] \left[\frac{d(\frac{\delta \sigma_2}{\sigma_2})}{dn_{qp}} \right] \left[\frac{dn_{qp}}{dT_{load}} \right] \left[\frac{dT_{load}}{dF_{src}} \right]$$

$$\frac{dS_{21}}{d(\frac{\delta f}{f})} = \frac{2Q^2}{Q_c}$$

$$\frac{d(\frac{\delta f}{f})}{d(\frac{\delta \sigma_2}{\sigma_2})} = \frac{\alpha}{2}$$

$$\frac{d(\frac{\delta\sigma_2}{\sigma_2})}{dn_{qp}} = \frac{1}{2N_0\Delta_0} \left[1 + \sqrt{\frac{2\Delta_0}{\pi kT}} e^{-\frac{\hbar\omega}{2kT}} I_0 \left(\frac{\hbar\omega}{2kT} \right) \right] = \kappa_2(\omega, T, \Delta_0)$$

$$\frac{dn_{qp}}{dT_{load}} = \frac{\eta \ k \ B}{RV\Delta_0(2n_{qp} + \frac{1}{R\tau_0})}$$

$$2kT_{src}\Delta\nu = F_{src}A_{tel}\eta_{tel}\Delta\nu \qquad \Longrightarrow \qquad \frac{dT_{load}}{dF_{src}} = \frac{\eta_{tel}A_{tel}}{2k}$$

What makes for a responsive MKID?

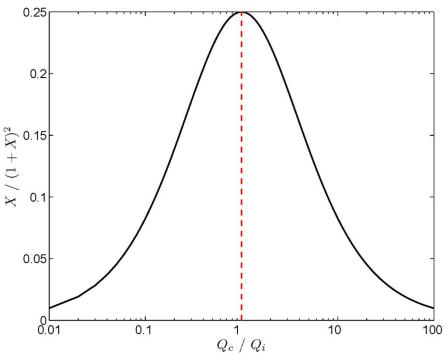
Responsivity =
$$\frac{\kappa_2(\omega, T, \Delta_0)}{\Delta_0} \left(\frac{\eta_{tel} A_{tel}}{2} \right) \left(\frac{\alpha}{V} \frac{\eta B}{(2Rn_{qp} + \frac{1}{\tau_0})} \right) \left(\frac{Q^2}{Q_c} \right)$$

Under typical loading conditions and bath temperatures $Rn_{qp}\gg rac{1}{ au_0}$

Neglecting the factors intrinsic to the material we are using (i.e. R, N₀, Δ_0) we obtain the following simplified expression:

Responsibility
$$\propto \frac{\eta B \alpha^2 Q_i^2}{V} \frac{X}{(1+X)^2}$$

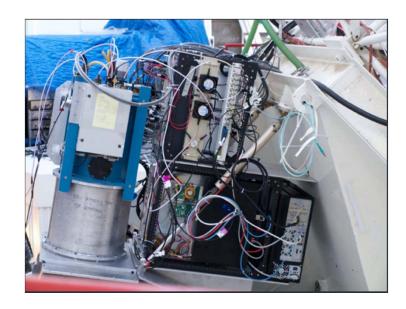
where
$$X = \frac{Q_c}{Q_i}$$

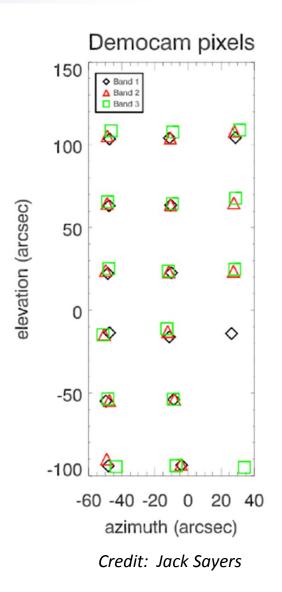


One year ago...

2010 Observing Run

- Beam shapes and locations matched expectations
- Successfully read out 100+ carriers (60 resonators)
- Demonstrated a path to the full-scale camera
- Plagued by low-frequency electronics noise
- Sensitivity 200-500 mJy s^{1/2}
- Factor of 10-100 above BLIP





The Problem of Dark Response

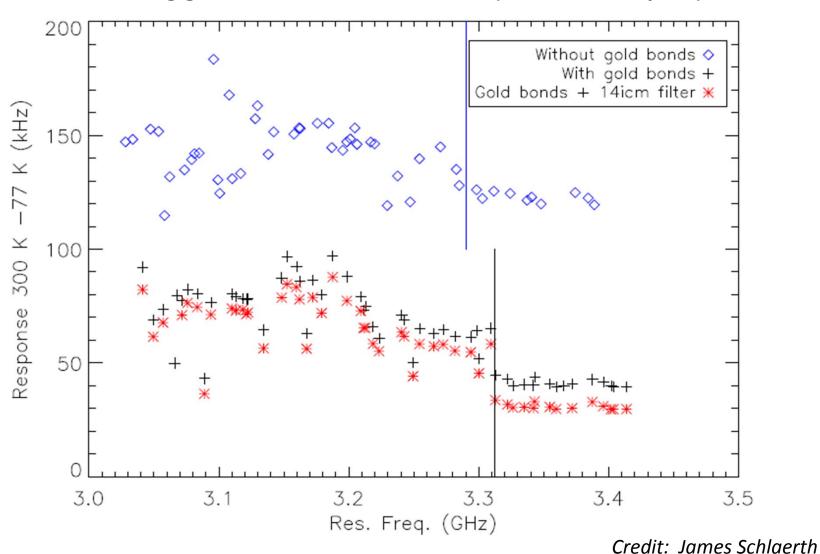
Resonators not-coupled to an antenna show significant response to outside-the-dewar loading.

Possible causes?

- Heating of the substrate
- Direct pick-up
 - Direct absorption in the aluminum section
 - Coupling through the interdigitated capacitor (IDC)

Substrate Heating

Result of adding gold wire bonds and 14 icm (420 GHz low-pass) filter

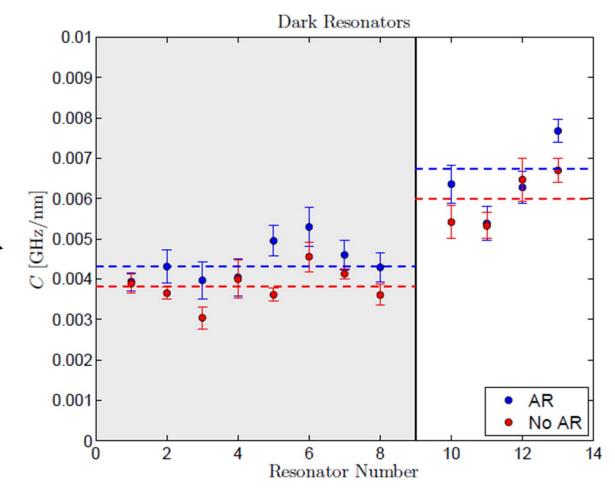


Half - Aperture Test

Placed aluminum aperture over half of the array.

Measured efficiency of the non-antenna coupled resonators.

$$C = \frac{\eta B}{d} \longrightarrow$$

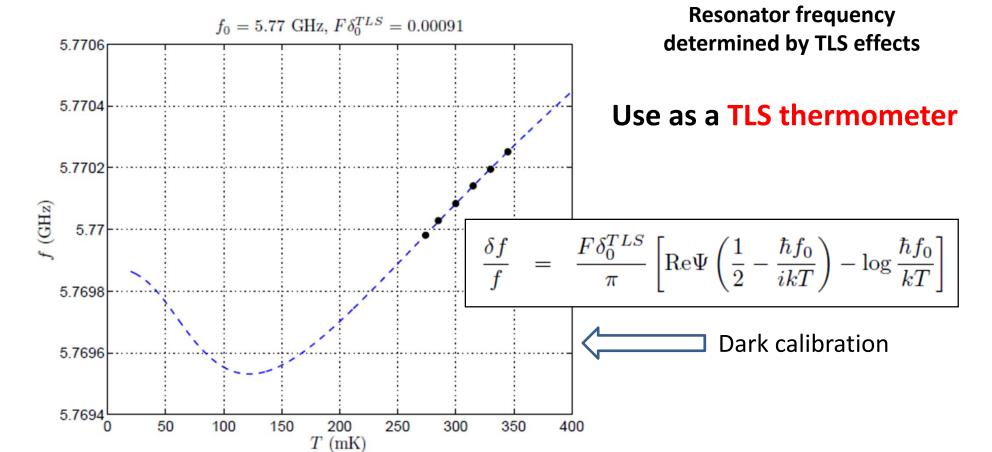


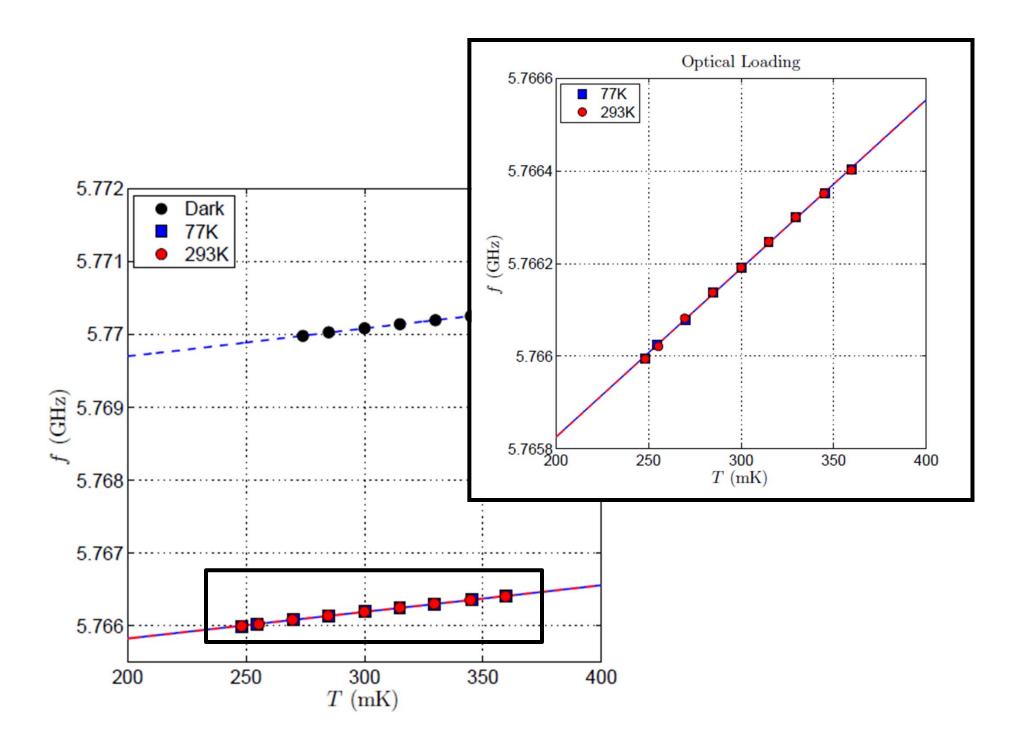
E Test Devices

$$T_c = 9.2 \text{ K}$$

$$\frac{2 \Delta}{h} \approx 700 \text{ GHz}$$

- Cannot absorb mm –radiation (no direct pick-up)
- Thermal quasi-particle density negligible





E Test Devices

 No change in the resonant frequency between 77K and 293K loads. Places tight upper-limit on the change in substrate temperature:

$$T_{293K} - T_{77K} \le 1.0 \text{ mK}$$

 The large response in our normal resonators between hot/cold loads simply cannot be explained by such a small change in substrate temperature.

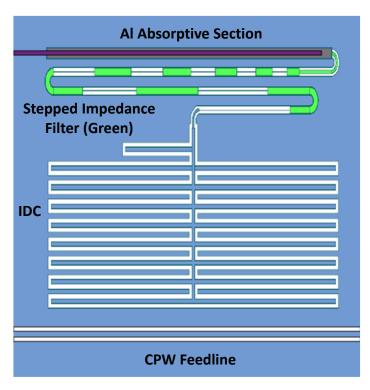
 Epsilon test devices also provide us with an estimate of the loss tangent of the dielectric

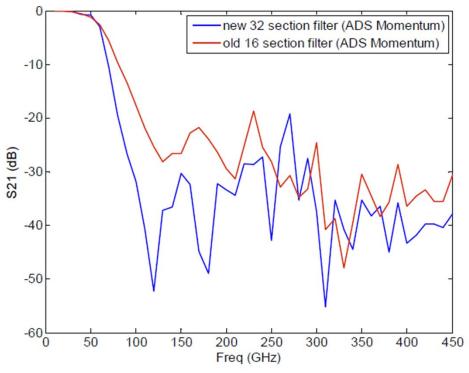
$$F\delta_0^{TLS} = 0.00085$$

 \circ And an estimate of the dielectric constant after simulating the magnetic inductance $L_{\rm m}$.

Coupling through the IDC

- Originally implemented IDC to reduce TLS noise
- Observed large increase in direct pick-up. Due to the geometry of the capacitor coupling to broadband radiation.
- Stepped impedance filter introduced between IDC and Al section to block frequencies
 80 GHz < v < 700 GHz





Credit: Omid Noroozian

Direct Pick-Up Device

- Currently testing a device without antennas
- Contains three groups of five resonators:
 - 1. IDC with 16-element stepped impedance filter
 - 2. IDC with new 32-element stepped impedance filter
 - 3. CPW
- o In each group the Al absorptive section is varied in length between 0 mm and 1 mm with the remainder Nb.
- o If pick-up is through the aluminum, the response should have some dependence on Al length.
- o If there is still pick-up through the IDC we should see drastic differences in the response between the three groups with **CPW < IDC-32 < IDC-16**

The Problem of Low Optical Efficiency

Not so much a problem as an insufficient understanding of the factors that effect the overall absorption of power in our detectors.

To this end we pursued:

- 1. A systematic characterization of all sources of loss in our system.
- Extensive hot/cold measurements, an improved model of our detectors, and a robust fitting procedure to obtain better estimates of the actual system efficiency.

Expected Efficiency

DemoCam

Band	Filters	Lyot Stop	Antenna Efficiency	Fringing Efficiency	Reflection at MKID	Phonon Emission	Overall Efficiency
0	0.73	0.18	0.42	0.69	1.0	0.66	0.025 +/- 0.005
1	0.76	0.36	0.47	0.68	1.0	0.58	0.05 +/- 0.01
2	0.73	0.52	0.49	0.76	1.0	0.58	0.08 +/- 0.02
3	0.68	0.63	0.41	0.96	1.0	0.58	0.10 +/- 0.02

MUSIC

Band	Filters	Lyot Stop	Antenna Efficiency	Fringing Efficiency	Reflection at MKID	Phonon Emission	Overall Efficiency
0	0.73	0.28	0.65	0.69	1.0	0.66	0.06 +/- 0.01
1	0.74	0.51	0.58	0.68	1.0	0.58	0.09 +/- 0.01
2	0.67	0.68	0.61	0.76	1.0	0.58	0.12 +/- 0.01
3	0.58	0.76	0.54	0.96	1.0	0.58	0.13 +/- 0.01

Full Model

Data

Hot /cold measurements of resonator frequency and quality factor made over a wide range of base temperatures (200 – 400 mK)

Model

Mattis-Bardeen Theory + Generation-Recombination Equation

Fit To

Frequency Shift

$$\Delta f(T) = f(T, 293K) - f(T, 77K)$$

and Naïve Excess Load

$$T_{exc}^{naive} = \frac{293/Q_i^2(T,77\text{K}) - 77/Q_i^2(T,293\text{K})}{1/Q_i^2(T,293\text{K}) - 1/Q_i^2(T,77\text{K})}$$

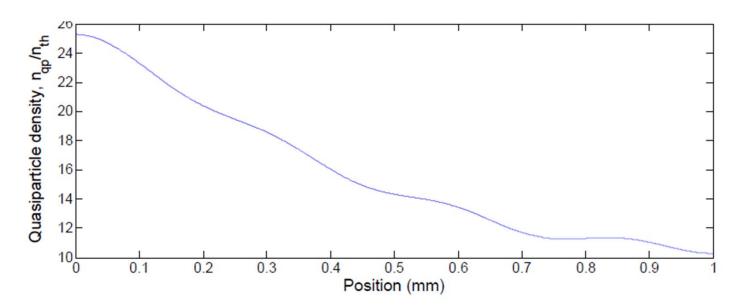
Full Model

 Allow for an elevated "effective temperature" T_{eff}, parameterized by a conductance law of the form

$$P=g$$
 $\left(T_{eff}^{eta}-T^{eta}
ight)$
5.5 × 10 -9 --- No Heating --- Heating --- Trick --- Heating --- 293K ---- Heating --- 293K ---- Heating --- 293K ---- No Heating --- Trick ---- Heating --- 293K ----- No Heating --- Trick ---- Heating --- 293K ----- No Heating --- Trick ---- Heating --- 293K ----- No Heating --- Trick ---- Heating --- 293K ----- No Heating --- Trick ---- Heating --- 293K ------ No Heating --- Trick ---- No Heating --- No Heating --- Trick ---- No Heating --- Trick ---- Heating --- 293K ------ No Heating --- Trick ---- No Heating --- No Heating --- Trick ---- No Heating --- Trick --- --- Tr

Full Model

o **Do not** take into account non-uniform absorption of radiation

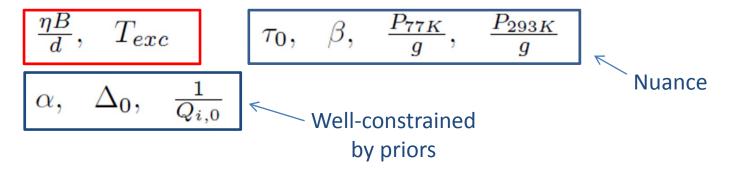


Credit: Jonas Zmuidzinas

Instead include a 1.15 correction factor to the efficiency obtained from the fit

Fitting Procedure

Total of 9 parameters, 3 have prior information from dark Mattis-Bardeen fits



- o Implement a MCMC using the **Metropolis Algorithm** and **simulated annealing** to efficiently explore the parameter space and search for global minimum of the likelihood function
 - Accounts for uncertainty in bath temperature, loading conditions, etc.
 - \circ Correctly capture the large correlation between α and Δ_0

Most Recent Results

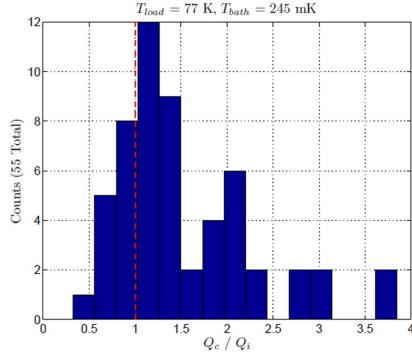
Array Description

Changes Made

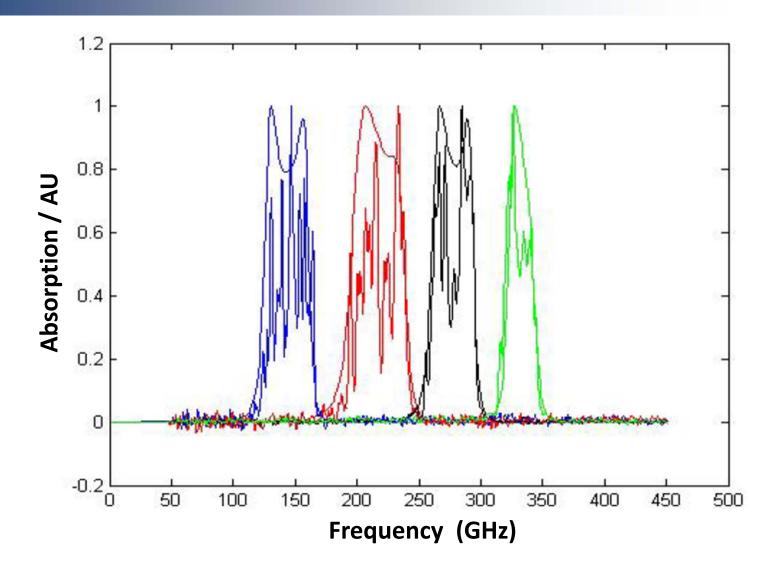
- Switched dielectric in microstrip and bandpass filters from SiO₂ to Si₃N₄
- Increased antenna slot and tap impedance for improved efficiency in lower frequency bands
- Included "index" and "loss" test devices to measure the phase velocity and loss in the microstrip
- Added a fourth band at 150 GHz (Band 0)

Broad Characteristics

- Approximately 100 out of 144 resonators survived (70% yield)
- Internal and coupling Q's well matched at base temperature under 77K load (comparable to sky loading at CSO).



Bandpasses



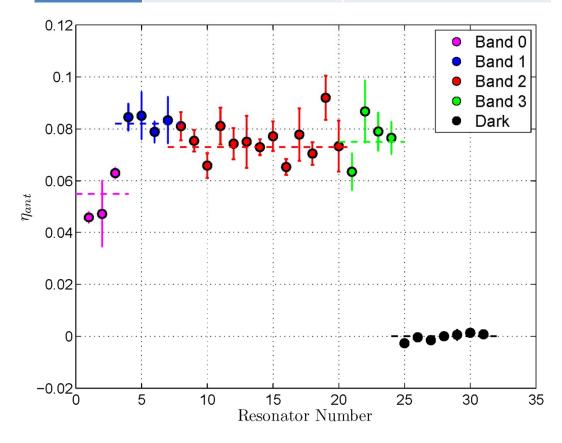
Epsilon of Si₃N₄:

7.0

Credit: Ran Duan

Optical Efficiency

Band	Expected Efficiency	Measured Efficiency
0	0.025 +/- 0.005	0.055 +/- 0.002
1	0.05 +/- 0.01	0.082 +/- 0.003
2	0.08 +/- 0.02	0.073 +/- 0.001
3	0.10 +/- 0.02	0.075 +/- 0.004



Note: Quoted uncertainties are only statistical. **Actually sensitive to**

$$\frac{\eta}{RV}$$

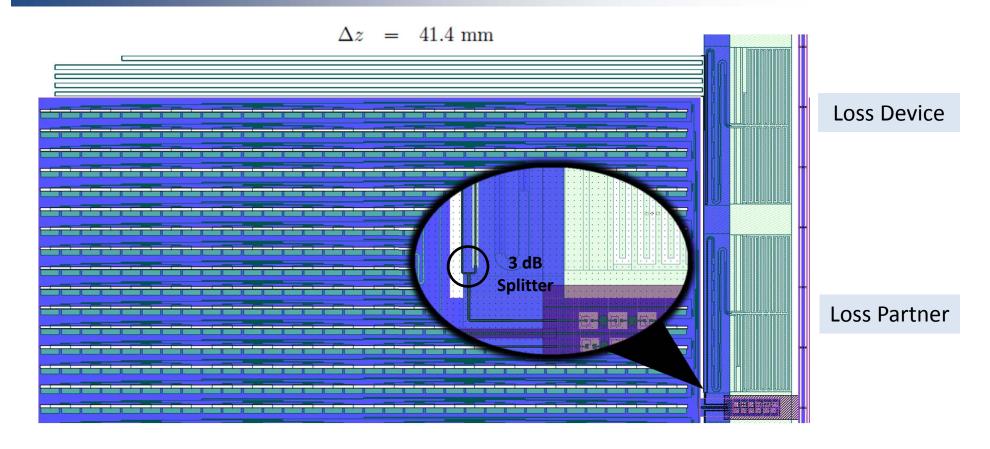
Assume that

$$R = 9.4 \ \mu \text{m}^3 \ \text{s}^{-1}$$

and

$$V = 1000 \ \mu \text{m} \times 6 \ \mu \text{m}$$
$$\times (55 \ \text{nm})$$

Loss Test Devices



Latest mask contained devices designed to measure the loss tangent of $\mathrm{Si_3N_4}$. These are based on devices designed by Chao-Lin Kuo for CMB polarization experiments, scaled to higher frequencies.

Loss Partner -- Loss Device efficiency ratio:

$$\eta_{LP} / \eta_L = 3.9 \pm 0.4$$

Loss tangent defined as the angle in the complex plane between the resistive component of an EM field and the reactive component

$$\tan \delta = \frac{\omega \epsilon'' + \sigma}{\omega \epsilon'}$$

Power dissipated in microstrip as:

$$P = P_0 e^{-\delta kz}$$



$$\delta = \frac{\ln\left(P_{LP}/P_L\right)}{k \ \Delta z}$$

Loss tangent of Si₃N₄:

$$\delta = 0.0016$$



8.4 mm of microstrip between antenna and device

Band	Transmission	
0	0.88	
1	0.83	
2	0.79	
3	0.75	

- o From epsilon test devices $F\delta_0^{TLS}=0.00085$
- o Roughly equal to previously measured values for SiO₂
- Factor of 2.25 larger than value measured in BICEP2 for Si₃N₄

Credit: Sunil Golwala

Excess Load

Load from the dewar being absorbed by our dark detectors:

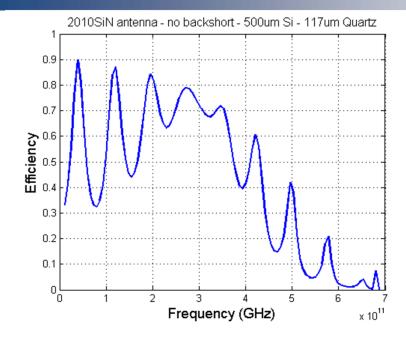
$$P_{dewar} = 0.4 pW$$

Load from the dewar being absorbed by our antenna coupled detectors:

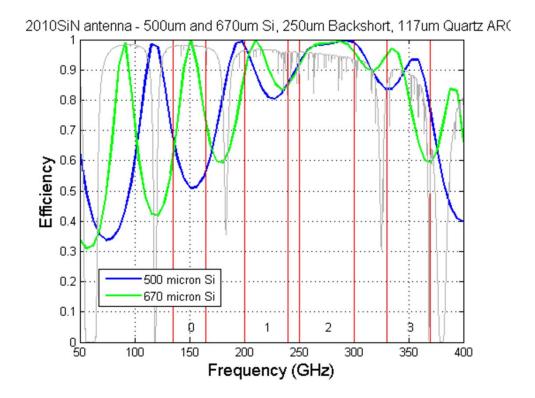
$$P_{dewar} = 1.0 - 1.5 pW$$
 (depending on band)

- o Corresponds to an excess load of 30 40 K
 - \circ 10 15 K due to direct pick-up
 - o 20 25 K due to antenna beam spilling onto inside of dewar

Nb Backshort





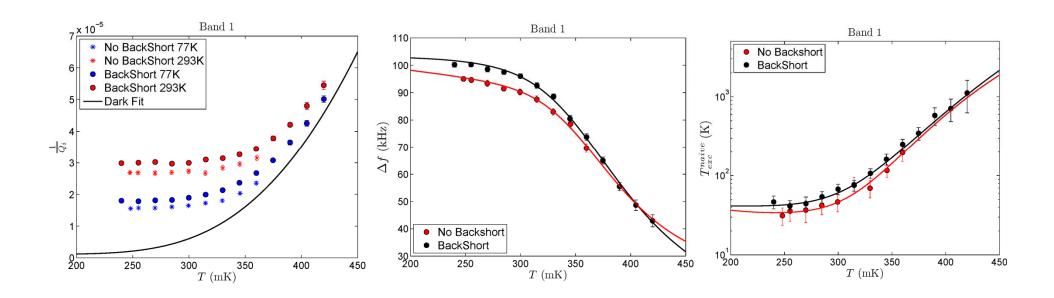


Credit: Peter Day

Current array has 500 μm Si with 117 μm Quartz AR Coat.

Implemented a 250 µm Nb backshort.

No Backshort vs. Backshort



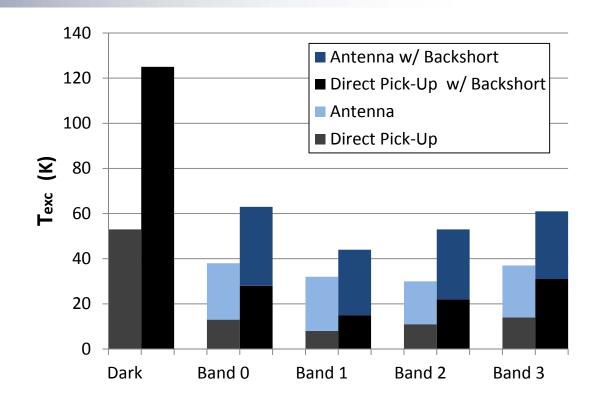
Improvement in optical efficiency

Band	Measured Efficiency	Measured Improvement	Expected Improvement
0	0.060	9%	-8%
1	0.099	21%	32%
2	0.085	17%	26%
3	0.093	24%	29%

o Efficiency of direct pick-up remained the same

No Backshort vs. Backshort

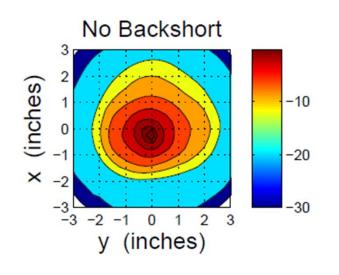
- Note that with the addition of the back short, we also blackened the inside of the magnetic shield
- We saw a large increase in excess load
 - P_{dewar} doubled for both dark resonator and antenna coupled resonators

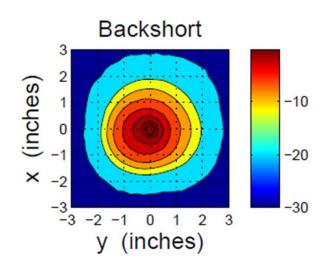


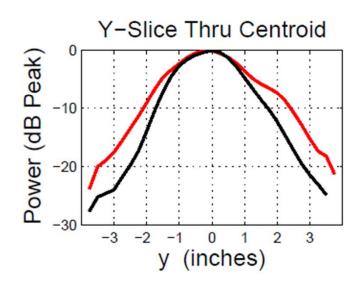
- Could be due to two competing effects
 - 1. Increased efficiency for direct absorption due to the backshort (increases η_{dir}).
 - 2. Decreased coupling to outside world due to blackening of the mag shield. Large angle response now terminates inside dewar (decreases η_{dir}).

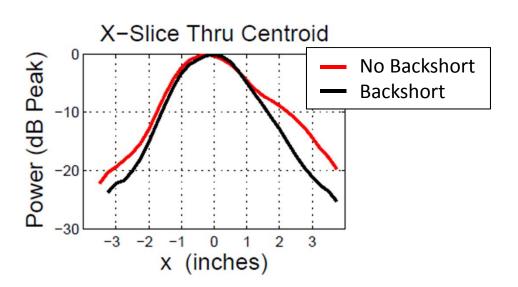
Beammaps

Stacked Map for Non-Antenna Coupled Resonators



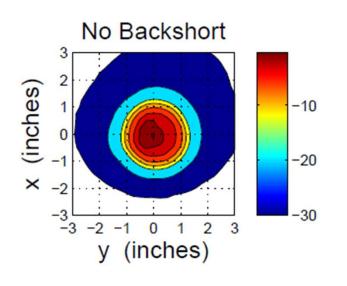


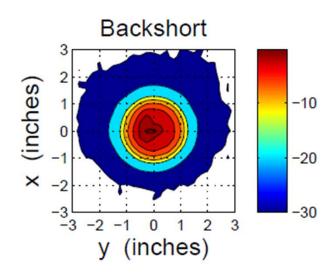


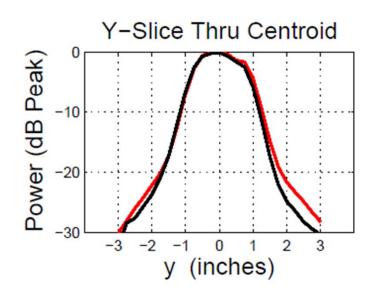


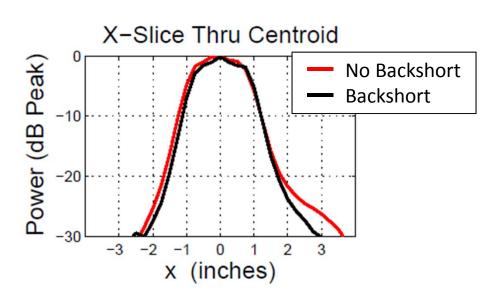
Beammaps

Stacked Map for Band 3 Resonators



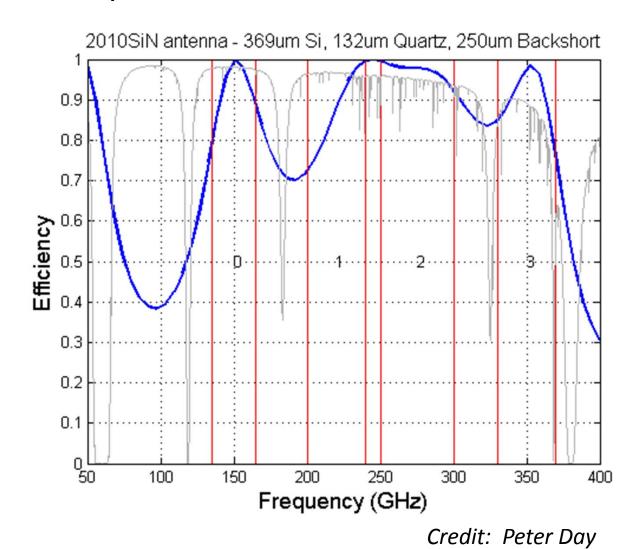






Nb Backshort

Room for improvement, particularly in Band 0. **Transmission for optimized Si and AR thickness:**



NEP

Defined as the signal power required to achieve a signal-to-noise ratio of 1.

$$NEP(\tilde{f}) = \sqrt{S_X(\tilde{f})} \left| \frac{dX}{dP_{\text{opt}}} \right|^{-1}$$

Dominant Sources of Noise:

o Photon:
$$\mathrm{NEP}_{\gamma}^2 = 2P_{\mathrm{opt}}h\nu_0 + \frac{2P_{\mathrm{opt}}^2}{\Delta\nu}$$

o Two Level System (TLS) noise:
$$S_{\delta f/f}^{
m TLS}(\tilde{f}) \propto T^{-2} \; P_{
m read}^{-1/2} \; \tilde{f}^{-1/2}$$

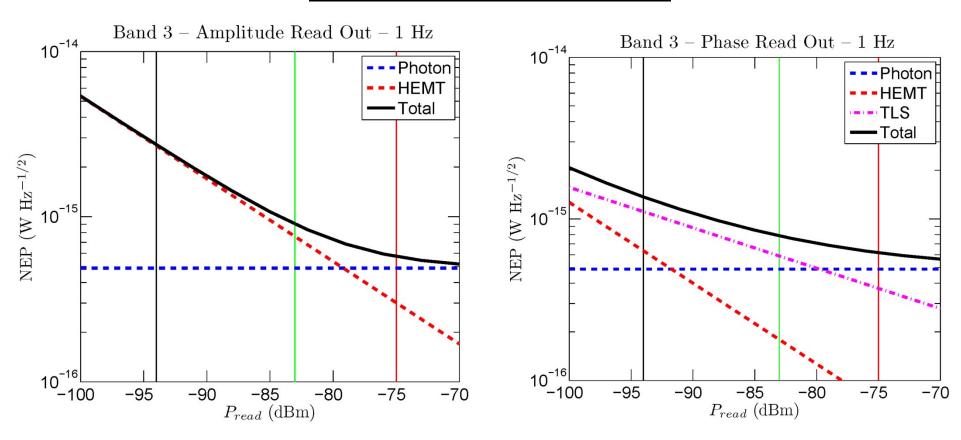
o HEMT noise:
$$S^{ ext{HEMT}}_{\delta ext{S}_{21}}(ilde{f}) = rac{kT_n}{2P_{ ext{read}}}$$
 where $T_n = 5 ext{ K}$

 Loading at CSO with MUSIC will be different from in lab, 77K load

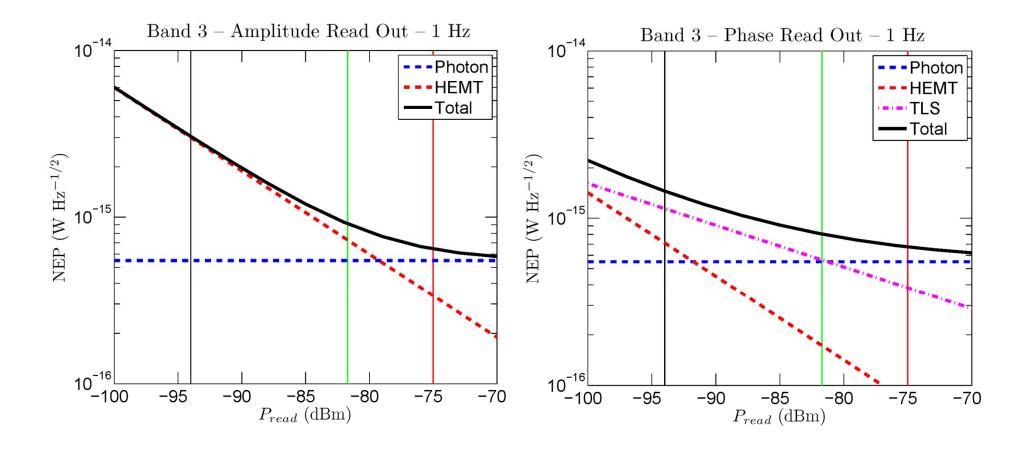
Band	Atmospheric Load
0	16 K
1	27 K
2	42 K
3	80 K

Credit: Jack Sayers

DemoCAM NEP -- No Backshort



DemoCAM NEP -- Backshort



In Conclusion...

Accomplishments

- Reduction of substrate heating (through the addition of gold wire bonds) to a negligible level (as measured by epsilon test devices).
- Better understanding of our optical efficiency.
 Measurements roughly match expectations!
- 15-25% improvement in efficiency with the introduction of a Niobium back-short (at the cost of increased excess load).
- Experimental results point to physics that we do not fully understand:
 - Anomalous frequency-to-dissipation ratio
 - Quasi-particle heating

Challenges

- Understanding the mechanism for direct pick-up
 - New "direct pick-up" mask currently being tested
- Optimizing MKID read-out power
- Removing correlated, low-frequency electronics noise
- Characterizing and reading out 2304 MKIDs

